

Strategies for Teaching **FRACTIONS**

Using Error Analysis for
Intervention and Assessment

David B. Spangler



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